

A Thesis Presented to  
The Faculty of Alfred University

EFFECTS OF POST-TREATMENT ABRASION ON DYNAMIC FATIGUE OF CHEMICALLY STRENGTHENED  
GLASS

by

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## ABSTRACT

Effects of post-ion exchange abrasion on strength and fatigue of soda-lime silicate glass rods, were determined using four-point bend tests. Dynamic fatigue tests were carried out by varying the strain rate over 2 orders of magnitude in air or after a short immersion in water. Ion exchange was carried out at 450°C for 4 or 16-hours. Following the ion exchange treatment, the glass rods were abraded using sand particles between 212 to 149 $\mu\text{m}$  and 106 to 63 $\mu\text{m}$ . The resulting strength (MOR) values were plotted using Weibull statistics. Dynamic fatigue plots showing the effect of stressing rate on strengths were also plotted, and the slow crack growth constant (n) was determined for each combination of ion exchange time and post-abrasion. Results indicate that the surface stresses induced by chemical strengthening reduces effects of stress-induced slow crack growth. However, anomalous, and unexpected large reductions in fatigue behavior requires that additional measurements, be carried out before any interpretations can be provided.

## INTRODUCTION

In glass science and engineering glass is often ion exchanged (IOX). This ion exchanging is a process of chemically strengthening a glass through diffusion of ions within the glass with an external ion source. “Ions from the glass diffuse out of the sample, while ions from the source diffuse into the sample”.<sup>1</sup> Sodium ions diffuse out while the potassium ions, from a molten  $\text{KNO}_3$  bath, are diffusing into the glass. It is the difference in size of these ions which allow for a chemically strengthening. Figure 1 contains an image of the glass surface after an IOX procedure has been completed.

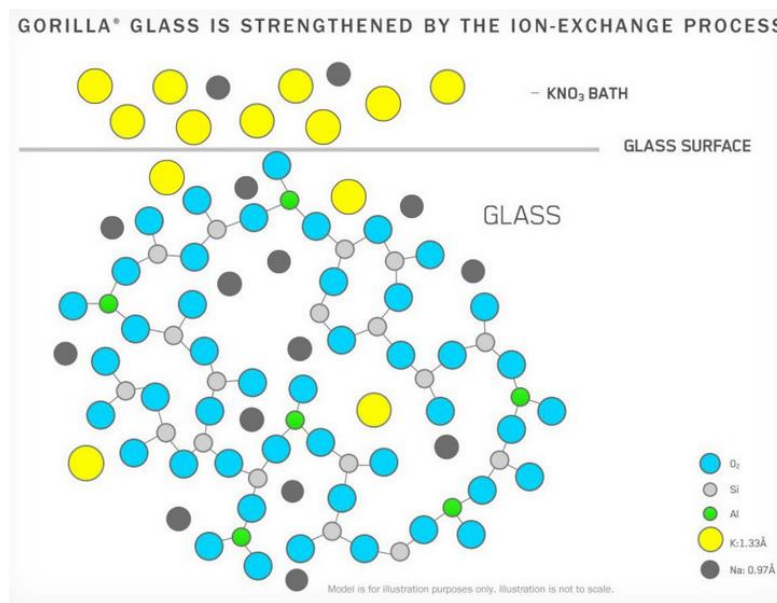


Figure 1: Ion-exchanged glass surface<sup>2</sup>

Glass is brittle material whose fracture behavior is dependent upon the surface flaws present. The strength at failure for glass depends if any treatments have been applied to the glass. The failure of glass is not determined by the bonding of the structure. Glasses fracture strengths are never able to reach their theoretical strengths due to surface flaws present on the glass. These surface flaws are detrimental to the possibility of a glass reaching its theoretical strength. The theoretical strength of a glass can be described by the following equation 1, in which  $E$  is the Young's or Elastic Modulus. As stated before, the theoretical strength will not be reached due to flaws located on the surface of the glass. “These flaws act as stress concentrations, increasing the local stresses to levels exceeding the theoretical strength and causing fracture of the glass”.<sup>1</sup>

Equation 1:  $\sigma_{theo} = \frac{E}{5}$

Griffith was able to account for the surface flaws and derived an expression to determine the glass failure, which is located in equation 2. This shows  $\sigma_f$  is the failure stress,  $\gamma$  surface energy, and  $c^*$  is the critical crack length of the crack growth. In order for a crack to grow it must reach the critical crack length.<sup>1</sup>

Equation 2:  $\sigma_f = \sqrt{\frac{2E\gamma}{\pi c^*}}$

There is variation in the glass fracture strengths due to the surface flaws. The crack tip propagation is dependent upon having a crack of suitable length and a stress great enough to grow the crack. The experimental method used to test the failure strength affects the value obtained. Three-point bend tests will receive a different failure strength than four-point bend tests. This is due to the area being tested during the failure strength test. The stress applied to the rods during the testing is maximum at different locations for the two tests. For “a 3-point bend test occurs at the point directly opposite the load point, while the maximum stress in a 4-point bend test occurs over the region between the two load points”.<sup>1</sup> The three-point bend tests have more variation in failure strengths due to the maximum stress at one point, when compared to the variation in the four-point bend test. “The probability of a critical flaw for a given stress occurring within the region of maximum stress is greater”.<sup>1</sup>

Due to the inability of determining an exact MOR for brittle solids failure statistics are used. Weibull distributions are used to describe the glass fracture strengths. The Weibull modulus has physical significance to the glass samples being tested and it is the distribution of the samples strengths. If the Weibull modulus is very large (infinite) then all the samples are breaking at one stress and is predictable. If the Weibull modulus is very small or low, then the samples are breaking at multiple stresses and is unpredictable. In general, it is best to have a large Weibull modulus because it shows that your sample is consistent and all break at the same stress/strength.

Static fatigue is when a constant load is placed on a glass sample until failure. The glass strength decreased with time, due to the atmosphere or moisture, interacting with the crack tip, which results in crack growth while the constant load is applied. A higher failure strength is



obtained when the load is increased at a fast rate. Meanwhile, when the load is increased at a slow rate the failure strength is lower. When the load rate is continually increased at a constant rate until failure, the glass is experiencing dynamic fatigue. Glass fatigue is due to the interaction of the glass surface flaw with water, which is also called stress-enhanced corrosion. This interaction can be described by equation 3. This shows the glass network displayed by the Si-O-Si bonds, which has oxygen acting as a bridging oxygen, and interacts with the water to form Si-OH. This Si-OH has the oxygen acting as a nonbridging oxygen and reduces the connectivity of the glass structure, specifically at the tip. This process can be found in Figure 2. The result of this interaction between the crack tip surface and water is a sharpening of the crack tip. This stress-enhanced corrosion of glass is influenced by the humidity, if there is a higher humidity then there is more water present and the reaction will likely drive to the right side in the creation of non-bridging oxygens. If the crack tip is under tension, then they are more prone to the chemical attack from the water. If there is a slower loading rate during strength testing, or static fatigue testing, then this reaction will have time to proceed and result in sharpening of the crack tip. Meanwhile, if the loading rate is faster the reaction will not have time to proceed and there will be no stress-enhanced corrosion occurring.<sup>1</sup>

Glass strengths are decreased through moisture and susceptible to static fatigue. In static fatigue, there is a constant load being applied to the sample for an extended period of time. During this process the glasses are susceptible to subcritical crack growth. “This leads to failure over time at loads which might be safe when considering instantaneous loading”.<sup>3</sup>

Equation 3:  $Si - O - Si + H_2O = 2 Si - OH$

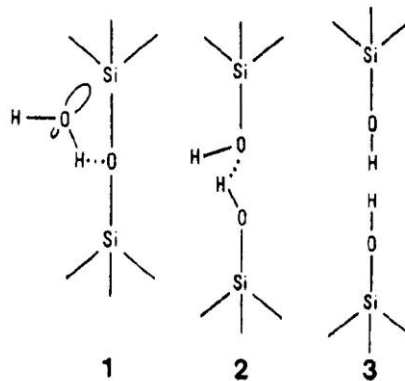


Figure 2: Stress-enhanced corrosion breaks the bonds at the crack tip, crack sharpening<sup>1</sup>

Glass and other brittle materials experience fracture through the rapid crack propagation. Fracture mechanics accounts for the relationships between numerous factors such as material properties, crack-producing flaws, stress levels, and crack propagation mechanisms. The fracture strength of brittle solids is much lower when compared to the theoretical strengths. This is due to the flaws or cracks present at the surface and interior of the solid. These flaws can be so crucial because an applied stress will be concentrated at the crack tip. The localized stress around the crack decreases as the distance from the crack increases. The Inglis equation, which is located in equation 4, approximates the maximum stress at the crack tip. Where  $\sigma_{tip}$  is the stress at the crack tip,  $\sigma_{ap}$  is the applied stress,  $\sigma_o$  is the applied tensile stress,  $r$  is the radius of curvature for the crack, and  $c$  is the length of the surface crack or half the length of the interior crack. The ratio of  $\sigma_{tip}/\sigma_{ap}$  is also termed the stress concentration factor  $K_{IC}$ , also called the critical stress intensity factor. This stress intensity factor “is simply a measure of the degree to which an external stress is amplified at the tip of a crack”.<sup>4</sup> The stress intensity factor can be described by equation 5.

$$\text{Equation 4: } \sigma_{tip} = 2\sigma_{ap} \left(\frac{c}{r}\right)^2$$

$$\text{Equation 5: } K_{IC} = \frac{\sigma_{tip}}{\sigma_{ap}} = 2 \left(\frac{c}{r}\right)^{1/2}$$

Dynamic fatigue has a sample continuously increasing stress at a constant rate until fracture. The slow crack growth constant or stress enhanced corrosion constant,  $n$  value, can be determined from a dynamic fatigue plot. A typical dynamic fatigue curve can be found below in Figure 3. The  $n$  value is affected by composition, environment, and state of stress. The slope of the curve would be  $m = 1/(n+1)$ . Sub-critical crack growth is when the crack is not a critical length for a fast fracture. However, the crack slowly grows until it reaches the crucial length required for failure. The environment and the crack velocity are in line with one another in for the slow crack growth region. Water is getting into the crack tip and slowly breaking the bonds and lengthening the crack. The slow crack growth constant shows how susceptible the glass is to slow crack growth or water assisted failure. The slow crack (sub-critical) crack growth equation can be found in Equation 6.

$$\text{Equation 6: } V = AK^n$$

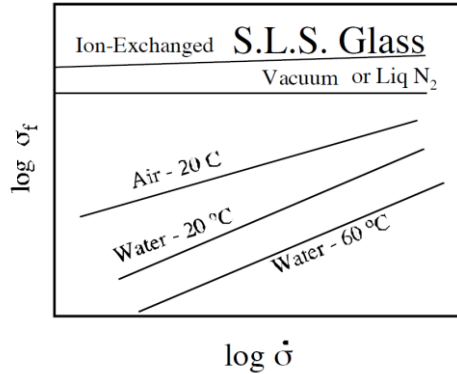


Figure 3: Typical dynamic fatigue curve

Glass fatigue is due to the interaction between glass and water, water reduces the connectivity of the glass and grows the crack. The  $n$  value represents how susceptible the glass is to water assisted failure. Strength decreases with time, due to moisture (humidity) or atmosphere interacting with the crack tip, the result is crack growth. If there is no water present, no chemical attack at the crack tip occurs. If the crack tip is in tension, then the crack is more prone to chemical attack. Soda-lime-silicate glasses typically have  $n$  values from 10 to 15.<sup>6</sup>

## EXPERIMENTAL PROCEDURE

The AR glass rods have a diameter of 4 mm and were cut to a length of three inches. The glass rods were tested in two mediums; air and water, and both will be discussed below in detail. The glass rods were ion-exchanged (IOX), abraded, and strength tested, in this order. The air medium had two IOX times, two sand particle size abrasions, and three testing rates. The water medium had one IOX time, one abrasion level, and three rates. In both medium cases strength testing for as received (nothing done to the glass), ion-exchange, and abrasion without ion-exchange was performed.

The ion-exchange (IOX) was performed in an Lindberg/Blue M Crucible Furnace, for either 4 or 16-hours at 450°C. The samples were loaded into a stainless steel sample holder, which can fit 100 samples, and were placed into a bath of KNO<sub>3</sub>. The IOX bath's temperature varies by  $\pm 10^\circ\text{C}$ , which, for present tests did not cause significant differences in treatments. The air medium had both the 4 and 16-hour ion-exchange bath times, while the water medium just had the 16-hour bath time.

Sand was used as the abrasive material. It was sieved using an auto tap W.S. Tyler Incorporated machine. The particle sizes collected from the sieve are as follows, in A.S.T.M. specification numbers; 30, 40, 70, 100, 120, 140, 230, and 325. In micrometer ( $\mu\text{m}$ ) mesh size; 595, 425, 212, 149, 125, 106, 63, and 45  $\mu\text{m}$ . The two particle sizes which were chosen to abrade the glass rods which were tested in the air medium are +149 and +63. The glass rods tested in the water had a particle size of +149 $\mu\text{m}$ . In which the + represents what sand particles which passed through the first mesh and were retained in the second mesh. The +149 sand particles have a range of 212 to +149 $\mu\text{m}$ , while the +63 sand particles have a range of 106 to +63 $\mu\text{m}$ . 400 grams of the specific sand particle size was placed inside of a jar mill. Ten samples were placed inside of the container at a time and were abraded (ABR) for fifteen minutes at a speed of 40% on a U.S. Stoneware Mill.

The glass rods were tested using a four-point bend test on a Instron. The support span length was 40 mm, while the load span length was 20 mm, giving the four-point bend test a span ratio of 2. The testing room is a climate-controlled environment, in which the relative humidity varies from 5% to 30%, depending on the weather for the specific day testing took place. The glass rod samples tested in air were tested at three different rates; 1, 7, and 20 mm/min.

Meanwhile the water strength tested rods had rates of 0.2, 2, and 20 mm/min. For the “water medium” samples, rods were submerged in water for a time of one to three minutes prior to the strength test, followed by fracture in air. The data for each test was recorded and the maximum flexure load was obtained, in order to determine the modulus of rupture (MOR), or  $\sigma_f$ .

To assure that the test procedure used above to determine water environment effects was valid, an additional test in which the glass was four-point bend tested in water was performed (Break in Water). These samples were abraded at +149 $\mu\text{m}$ , and abrasion before an IOX in combination, and were tested at a rate of 2 mm/min.

## DATA

Following the completing of the four-point bend tests, which determine the maximum flexural load, the modulus of rupture (MOR), or the stress at failure ( $\sigma_f$ ), can be calculated. The MOR can be determined by equation 7. In which P is the maximum flexure load [N], D is the diameter [D], L is the support length span [mm], a is the load length span [mm], and the MOR is in units of MPa. The maximum flexure load and MOR for both testing mediums, along with the average and standard deviation for MOR can be found in the Appendix.

$$\text{Equation 7: } MOR = \frac{8P(L-a)}{\pi D^3}$$

A Weibull “probability of failure” plot was created for each specific testing condition including the rate at which the samples were tested. Weibull plots can be created using the MOR value and F, where F is the “probability of failure at a particular stress” and equals the “number of samples failing at a specific stress minus 0.5 divided by the total number of samples”. (Equation 8). The y-axis of a Weibull modulus contains F, specifically  $\ln(\ln(1/(1-F)))$ , and the x-axis contains the  $\ln(\text{MOR})$ . Once the Weibull plot has been created if a linear trendline for the data is created (e.g. the slope of the data) for each specific group and testing rate. The slope is the Weibull modulus, “m”, and is a measure of the scatter in the data. All Weibull moduli can be found in Table 1.

The n value, or stress enhanced carrion or slow crack growth constant, can be determined by taking the average MOR for each testing rate for a specific group and plotting it. The y-axis is  $\log(\sigma_f)$  and the x-axis is  $\log(\sigma_{\text{rate}})$ . Following the creation of the plot a trendline is added, in which using the slope of the line (m) (Equation 9) one can determine the n value by following equation 10.

$$\text{Equation 8: } F = \frac{(\# \text{ failing at } \sigma - 0.5)}{N}$$

$$\text{Equation 9: } \text{slope } (m) = \frac{1}{(n+1)}$$

$$\text{Equation 10: } n = \frac{1}{m} - 1$$

The Weibull plot for all samples tested in air and which were as just received (AR), ion exchanged (IOX), or just abrasion (ABR) at the different stress rates can be found in Figure 4.

This figure allows for each comparison of Weibull modulus and the failing strength for each different type of sample. Figure 5 contains the Weibull plot for the samples which had the combination of ion exchanging followed by abrasion for all testing rates. Finally, the water Weibull plot for the samples which were submerged in water for one to two minutes before testing can be found in Figure 6.

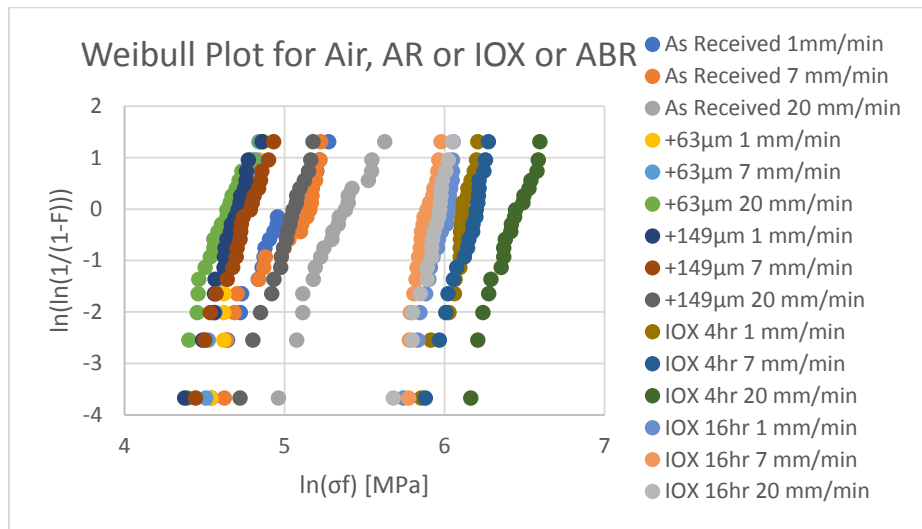


Figure 4: Weibull Plot for air testing of samples with either as received, just abrasion, or just ion exchange

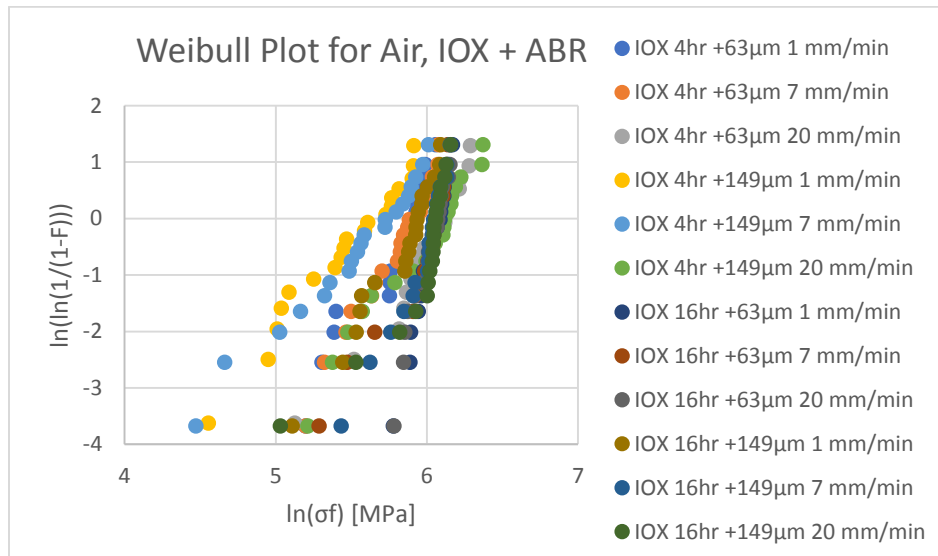


Figure 5: Weibull plot for air testing of samples with the combination of ion exchanging followed by abrasion

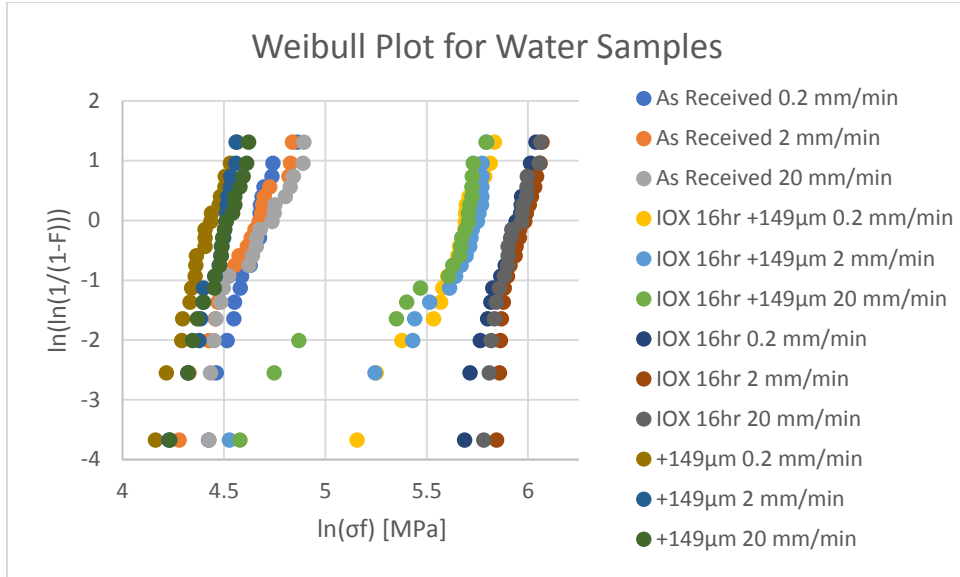


Figure 6: Weibull plot for the water samples as received, just ion exchange or abrasion and then the combination

The dynamic fatigue plots for the as received, just IOX, or just ABR can be found in Figure 7. This figure, when the axes are both on a LOG scale can be used to calculate the  $n$  value. Figure 8 contains the dynamic fatigue plot for the samples which were IOX and ABR tested. Meanwhile the samples which were submerged in water before breaking have their dynamic fatigue plot in Figure 9.

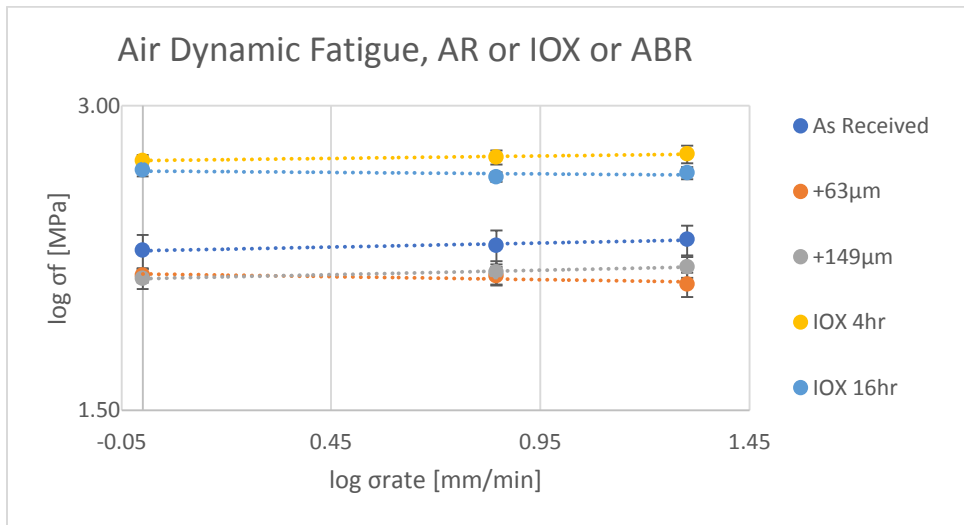


Figure 7: Dynamic fatigue plot for the water testing of as received, just abrasion or just ion exchange



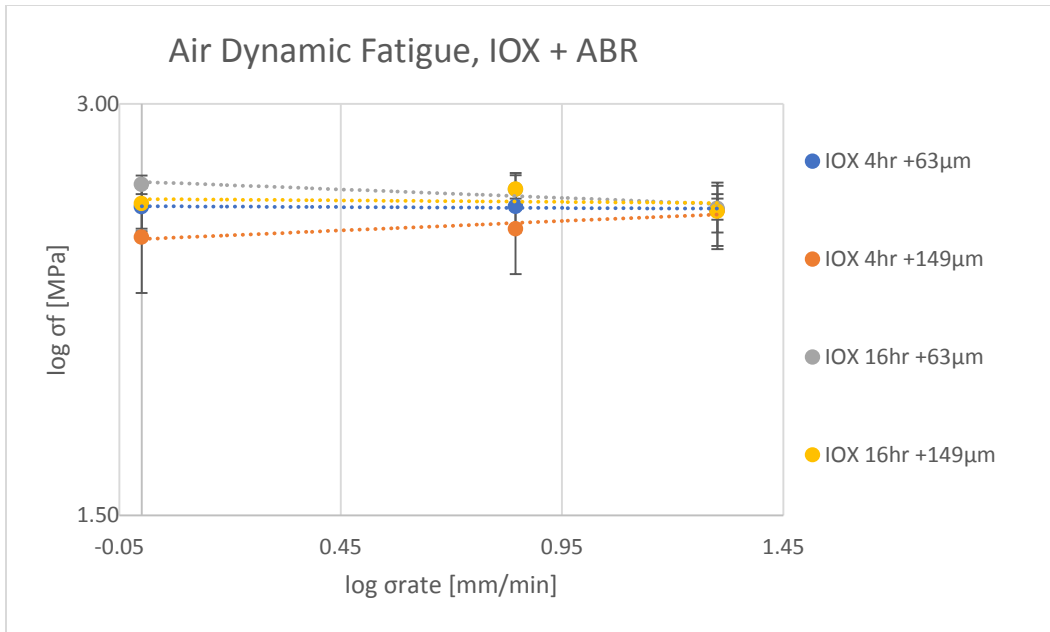


Figure 8: Dynamic fatigue plot for air testing of samples which were abraded and then ion exchanged

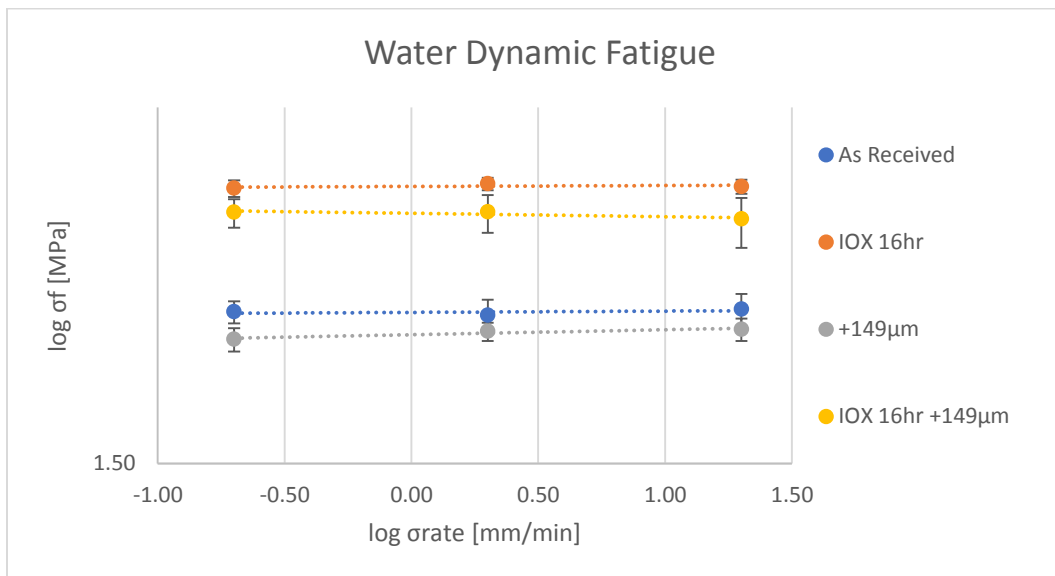


Figure 9: Dynamic fatigue plot for the water samples

Table 1: Three different m values for each rate, along with the n value for each group tested

| Group           | Air         |        |       |         |          |               |                |                |                 | Water       |          |       |                 |
|-----------------|-------------|--------|-------|---------|----------|---------------|----------------|----------------|-----------------|-------------|----------|-------|-----------------|
|                 | As Received | 63µm   | 149µm | IOX 4hr | IOX 16hr | IOX 4hr +63µm | IOX 4hr +149µm | IOX 16hr +63µm | IOX 16hr +149µm | As Received | IOX 16hr | 149µm | IOX 16hr +149µm |
| m (slow rate)   | 6.10        | 14.82  | 11.07 | 13.59   | 13.97    | 4.70          | 3.17           | 12.33          | 4.76            | 11.88       | 12.31    | 11.77 | 6.87            |
| m (medium rate) | 5.61        | 11.79  | 9.26  | 11.61   | 18.42    | 4.87          | 2.89           | 5.05           | 6.60            | 7.75        | 16.07    | 14.25 | 3.76            |
| m (fast rate)   | 6.92        | 9.28   | 10.34 | 9.55    | 13.89    | 4.30          | 3.69           | 11.22          | 4.15            | 7.37        | 14.71    | 11.99 | 3.19            |
| n               | 23.69       | -37.10 | 23.33 | 33.48   | -57.82   | -127.58       | 11.85          | -14.57         | -77.92          | 191.31      | 211.77   | 52.76 | -62.73          |

Figure 10 contains the Weibull plot for the samples which were just ABR and then ABR followed by IOX. These samples were submerged in water before breaking (submerge) and the samples which were tested under water and broke while being in the water (brake). Table 2 supplies the m values for these submerged and brake samples tested at the 2mm/min. Note, n values couldn't be obtained due to the samples being tested at only one rate.

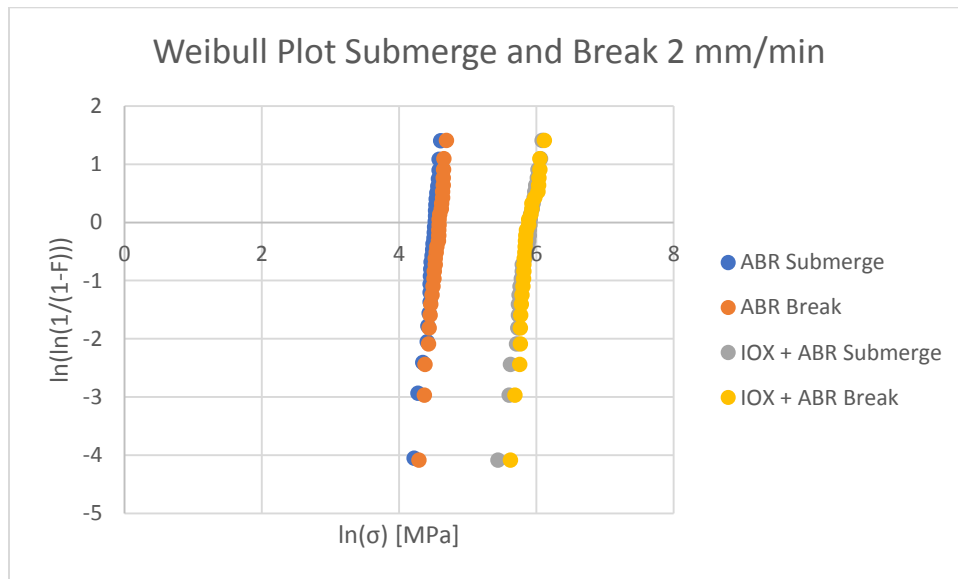


Figure 10: Break in Water Weibull Plot

Table 2: m values for addition testing of submerged and breaking in water samples

| m value | Submerged in Water |                  | Break in Water |                  |
|---------|--------------------|------------------|----------------|------------------|
|         | 149µm              | 149µm + IOX 16hr | 149µm          | 149µm + IOX 16hr |
|         | 14.02              | 8.57             | 12.91          | 10.03            |

## RESULTS

The glass used for this thesis is AR Glass, which is produced by Schott. AR glass is a unique type of soda -lime-silicate glass whose chemical composition is as follows 69% SiO<sub>2</sub> 1% B<sub>2</sub>O<sub>3</sub> 3% K<sub>2</sub>O 4% Al<sub>2</sub>O<sub>3</sub> 13% Na<sub>2</sub>O 2% BaO 5% CaO 3% MgO. The main components are in approximate weight percent.<sup>5</sup>

As a glass is ion exchanged, the stress enhanced corrosion or slow crack growth constant (n) increases. The longer the ion exchange time, the larger compressive stress is added to the glass surface and the larger the n value obtained. For every order of magnitude in which the loading rate is increased, the glass will fail at a stress that is 40% larger than the previous failure stress. Figure 11 shows that the theoretical dynamic fatigue curve and Table 3 shows the theoretical n values. The n values approximately increase by a total of 3 when the compressive stress, influenced by ion exchange time, is increased by 100MPa.

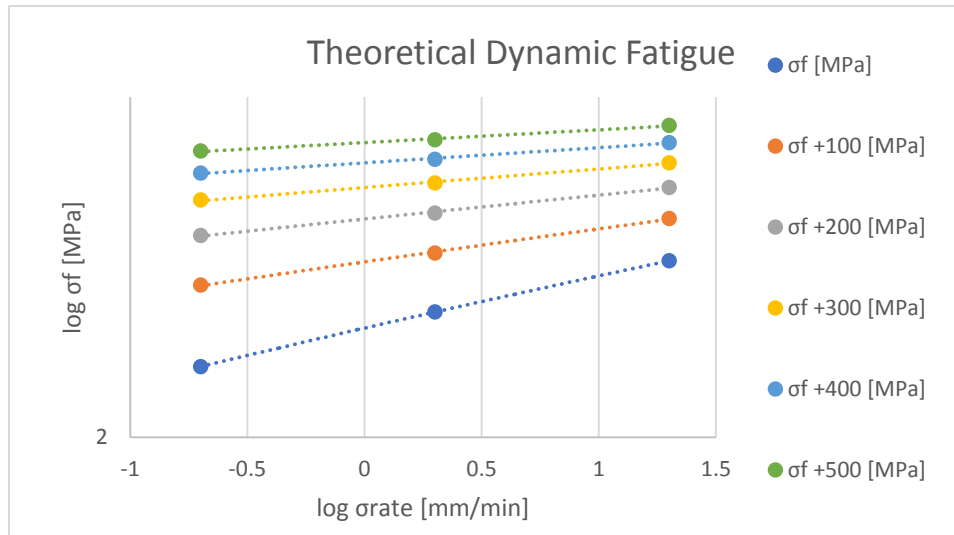


Figure 11: Theoretical Dynamic Fatigue Plot

Table 3: Theoretical n Values

|                  | n value |
|------------------|---------|
| $\sigma_f$       | 5.8     |
| $\sigma_f + 100$ | 9.1     |
| $\sigma_f + 200$ | 12.4    |
| $\sigma_f + 300$ | 15.6    |
| $\sigma_f + 400$ | 18.8    |
| $\sigma_f + 500$ | 22.0    |

Both treatments, the IOX and abrasion, impacted the strengths of the glass. The abrasion, as expected weakened the glass, and the IOX increased the glass strength. The abrasion lowered the strength of the glass, regardless of testing, by approximately 25 to 50 MPa. Meanwhile the IOX treatment increased the strength of the glass generally by about a minimum of 200 MPa. The testing rates which were used didn't impact the strength of the glass to a large extent. The faster testing rates didn't always provide larger results, and when it did provide larger strengths it was only by a few MPa.

The Weibull moduli shows if the glass is consistently breaking at the same stress or not. The larger the Weibull moduli (slope of m) the more consistent the glass strength. Between the testing rates for the glass groups which had the same alterations made to it, the Weibull moduli is inconsistent.

The characteristic strength can be determined when the y-axis is equal to zero on a Weibull modulus figure. When  $\ln(\ln(1/(1-F))) = 0$  that is defined as the characteristic strength. This characteristic strength can be used to compare strength values of different Weibull moduli.

It was previously stated that for every order of magnitude in loading rate in which the glass is tested the glass should break at a stress 40% greater than the previous stress. In the failure strengths obtained, this 40% increase in strength is not observed. This brings into question the loading rate and how the strengths did not change, when ideally the faster rates should have larger strengths. When the glass is being tested at a slower loading rate there is more time for interaction between the crack tip and the water. Ideally the water should grow the crack and

interact. Meanwhile if the glass is being tested at a faster rate then there is no time for an interaction between the crack tip and water. It is possible that the IOX treatment was not allowing for water to reach the crack tip, and as a result there would be no lengthening of the crack and no water assisted failure.

The  $n$  values obtained do not with the theoretical  $n$  values, which range between 5 to 20, which do not match that of the measured values. The measure  $n$  values are also very inconsistent, ranging from about 200 to about -125 depending on which samples are being observed. A negative  $n$  value would suggest that the glass is getting stronger while aged under stress. Positive  $n$  values indicate that the glass is getting weaker under stress and with an increase in time. Overall a larger positive  $n$  value means that the glass is less susceptible to slow crack growth, while a smaller positive  $n$  value shows the glass is more susceptible to slow crack growth. The IOX 4hr + 63 $\mu$ m, IOX 4hr, and 149 $\mu$ m, all of which were tested in air, had the most reasonable  $n$  values of all the tested groups. If there is no water present there will be no attack on the crack tip, even if the glass is sensitive to water. For the groups tested which have large  $n$  values, it could be possible that the water is not reaching the crack tip, due to the IOX treatment which was done to the glass, so no stress enhanced corrosion is occurring in the first place.

The observed slow crack growth constant,  $n$ , do not match that calculated from the theoretical. This shows that the theoretical data used to determine what the  $n$  value is incorrect. It is difficult to predict the  $n$  value when multiple variables are used. The theoretical data only takes into account the IOX time period, due to the corresponding compressive stress placed on the surface of the glass. The theoretical value does not consider the abrasion or introduction of flaws on the surface of the glass. The combination of both ion exchange and abrasion change the distribution of flaws present on the surface.

A possible issue in the experiment is a a possible inconsistency in the humidity in the mechanical testing room, it is a “controlled humidity”. However, the humidity reader has been found to be incorrect with providing the actual humidity. If some samples were tested in more humid days, then those samples would have possibly had more interactions between water and the crack tip.

The  $n$  value as a function of sample type and the treatment done to the samples can be found in Figure 12. This figure shows the inconsistency of the  $n$  value. The Weibull moduli for

both the air and water samples as a function of loading rate can be found in Figures 13 and 14. These figures show that the modulus is inconsistent between the three different loading rates. The characteristic strength as a function of loading rate for both the air and water samples can be found in Figure 15 and 16. The characteristic strength has little change depending on the loading rate, which is not what is expected. This shows that there is no change in strength as you increase the loading rate, the faster rates are not stronger than the slower rates.

The data regarding the samples which were tested after submerging in water and then testing and breaking in water supplies some interesting information. From the data it can be determined that there is a small difference between testing after the samples were submerged in water for a few minutes before breaking and testing while the rods were immersed in water for the testing.

Recent data obtained just before the final due date for the thesis indicates a possible additional affect on measured strength, this data can be found in Table 4. The data is ball on ring testing done by a Budziszewski. The data obtained for this thesis, along with the data obtained by Budziszewski, might possibly provide an answer for the unusually high n values and negative n values. It is possible that the Instron load cell is not recording the actual breaking strength at high load rates.

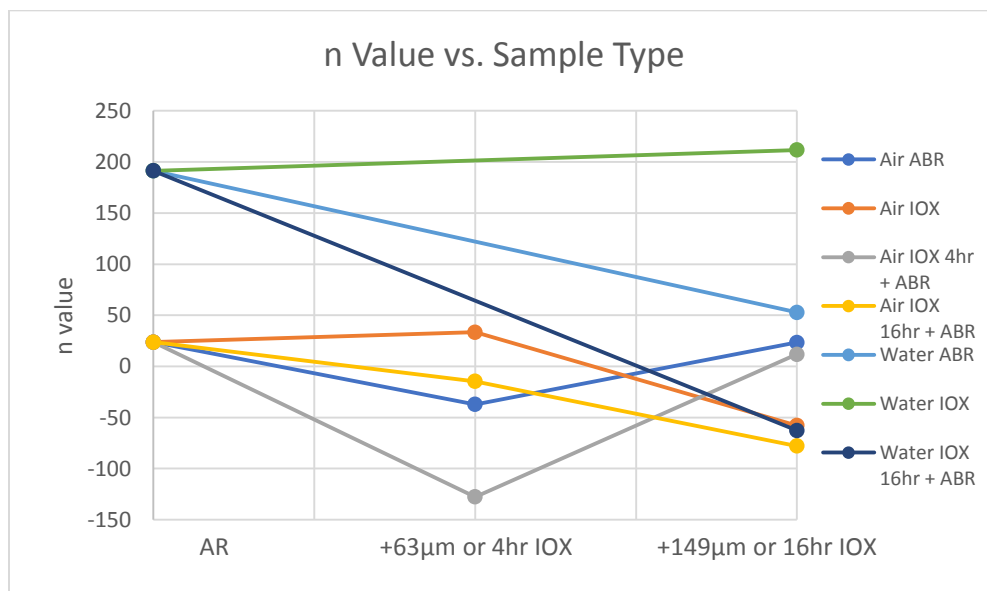


Figure 12: The n value as a function of sample

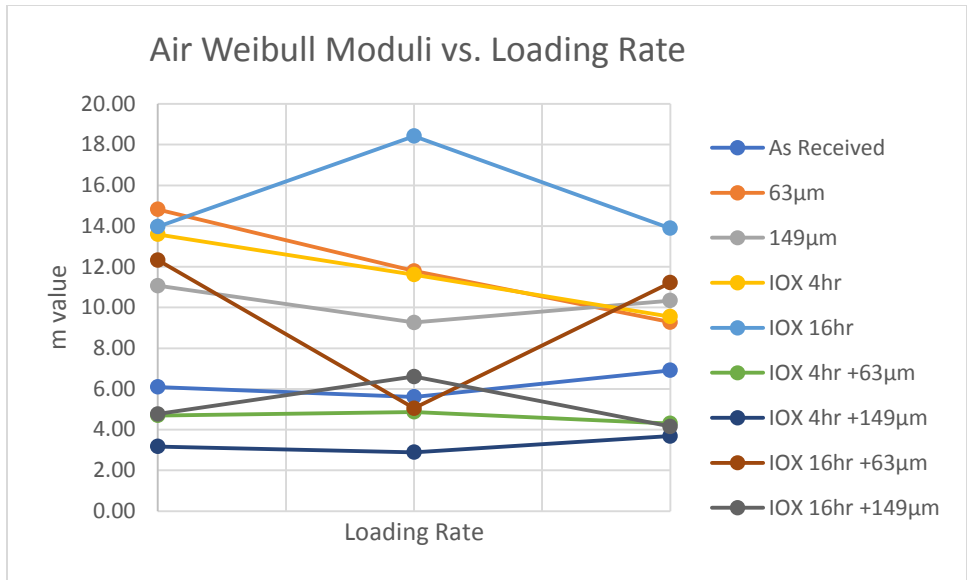


Figure 13: Weibull modulus for samples tested in air as a function of loading rate

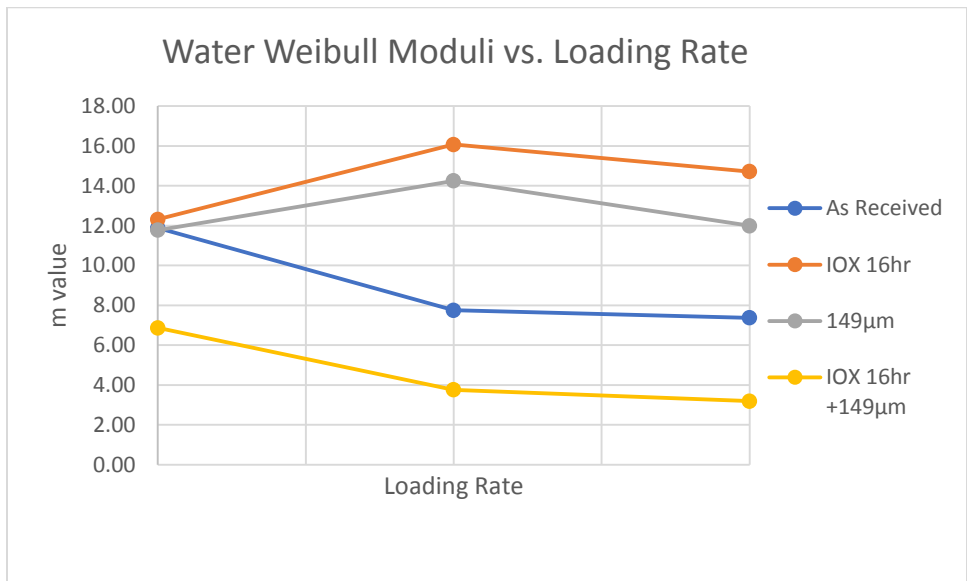


Figure 14: Weibull modulus for water samples as a function of loading rate

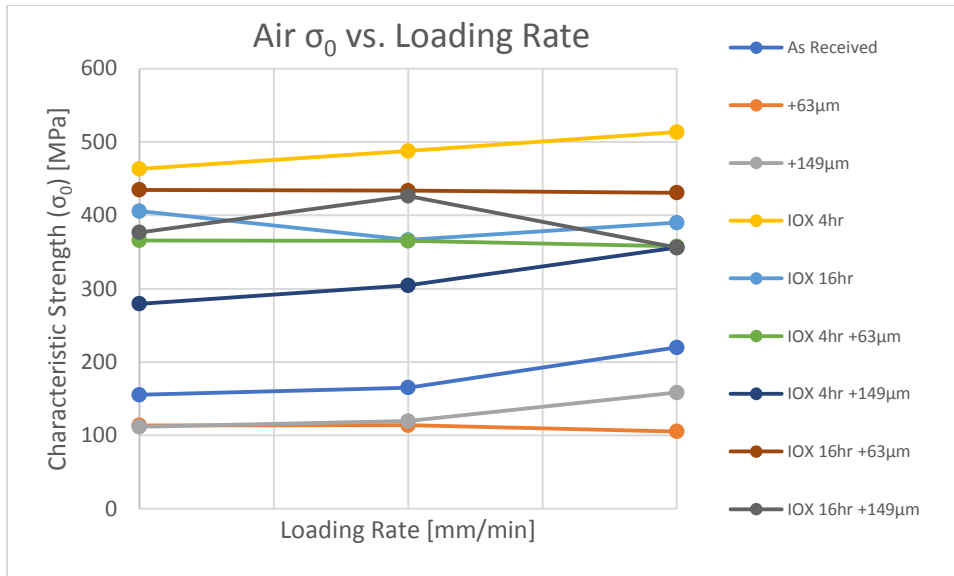


Figure 15: Air sample characteristic strength as a function of loading rate

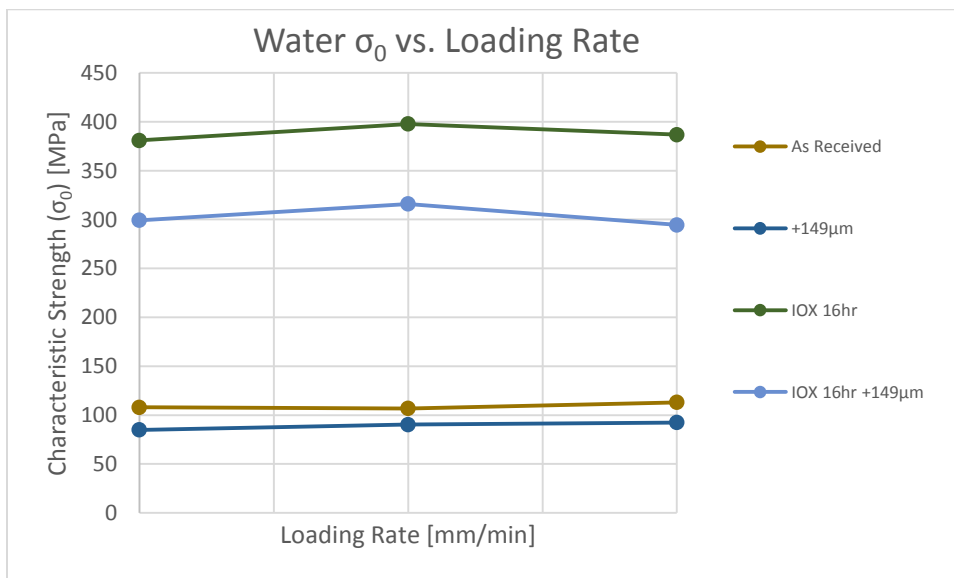


Figure 16: Water sample characteristic strength as a function of loading rate

Table 4: Ball on ring test data

| mm/min | Mean MOR | St. Dev. |
|--------|----------|----------|
| 0.7    | 166.8    | 16.3     |
| 7      | 168.7    | 21.7     |
| 70     | 124.1    | 14.9     |



## CONCLUSION

The surface stresses induced through chemical strengthening by ion exchange reduced the effect of stress-induced slow crack or water is restrained from interacting crack tip. The data was expected followed the expected theoretical data, in which for every order of magnitude of an increase in testing rate the glass fails at a stress that is 40% larger than the previous strength. The model which is used to calculate this data could be incorrect. The n value is difficult to predict when both IOX and abrasion is altered, in combination both the IOX and abrasion change the flaw distribution.

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APPENDIX

Table A1: Air as Received Glass Data

| None     |        |          | None     |        |          | None      |        |          |
|----------|--------|----------|----------|--------|----------|-----------|--------|----------|
| 1 mm/min |        |          | 7 mm/min |        |          | 20 mm/min |        |          |
| P        | MOR    |          | P        | MOR    |          | P         | MOR    |          |
| 1        | 117.93 | 93.89331 | 1        | 128.06 | 101.9586 | 1         | 143.09 | 113.9252 |
| 2        | 130.57 | 103.957  | 2        | 129.57 | 103.1608 | 2         | 160.24 | 127.5796 |
| 3        | 141.61 | 112.7468 | 3        | 136.35 | 108.5589 | 3         | 166.51 | 132.5717 |
| 4        | 142.58 | 113.5191 | 4        | 138.78 | 110.4936 | 4         | 166.53 | 132.5876 |
| 5        | 158.17 | 125.9315 | 5        | 159.06 | 126.6401 | 5         | 177.72 | 141.4968 |
| 6        | 162.07 | 129.0366 | 6        | 163.82 | 130.4299 | 6         | 180.06 | 143.3599 |
| 7        | 164.06 | 130.621  | 7        | 165.25 | 131.5685 | 7         | 186.32 | 148.3439 |
| 8        | 165.04 | 131.4013 | 8        | 186.25 | 148.2882 | 8         | 189.99 | 151.2659 |
| 9        | 169.72 | 135.1274 | 9        | 191.69 | 152.6194 | 9         | 199.61 | 158.9252 |
| 10       | 174.65 | 139.0525 | 10       | 206.01 | 164.0207 | 10        | 201.05 | 160.0717 |
| 11       | 178.16 | 141.8471 | 11       | 207.73 | 165.3901 | 11        | 207.89 | 165.5175 |
| 12       | 178.55 | 142.1576 | 12       | 214.57 | 170.836  | 12        | 209.22 | 166.5764 |
| 13       | 196.84 | 156.7197 | 13       | 218.25 | 173.7659 | 13        | 217.37 | 173.0653 |
| 14       | 206.45 | 164.371  | 14       | 220.56 | 175.6051 | 14        | 221.02 | 175.9713 |
| 15       | 207.36 | 165.0955 | 15       | 221.67 | 176.4889 | 15        | 221.18 | 176.0987 |
| 16       | 207.91 | 165.5334 | 16       | 221.8  | 176.5924 | 16        | 226.5  | 180.3344 |
| 17       | 218.21 | 173.7341 | 17       | 226.62 | 180.4299 | 17        | 251.07 | 199.8965 |
| 18       | 228.27 | 181.7436 | 18       | 227.25 | 180.9315 | 18        | 255.66 | 203.551  |
| 19       | 232.05 | 184.7532 | 19       | 232.9  | 185.4299 | 19        | 256.25 | 204.0207 |
| 20       | 245.83 | 195.7245 | 20       | 234.04 | 186.3376 | 20        | 277.95 | 221.2978 |
|          | SUM    | 2886.967 |          | SUM    | 3049.546 |           | SUM    | 3276.457 |
|          | AVG    | 144.3483 |          | AVG    | 152.4773 |           | AVG    | 163.8229 |
|          | STD    | 27.52026 |          | STD    | 29.06089 |           | STD    | 27.90502 |

Table A2: Air +63µm Glass Data

| AB +63 1 mm/min |        |          | AB +63 7 mm/min |        |          | AB +63 20 mm/min |        |          |
|-----------------|--------|----------|-----------------|--------|----------|------------------|--------|----------|
| P               | MOR    |          | P               | MOR    |          | P                | MOR    |          |
| 1               | 117.79 | 93.78185 | 1               | 114.01 | 90.77229 | 1                | 101.97 | 81.18631 |
| 2               | 127.49 | 101.5048 | 2               | 115.78 | 92.18153 | 2                | 102.49 | 81.60032 |
| 3               | 127.55 | 101.5525 | 3               | 120.76 | 96.1465  | 3                | 108.04 | 86.01911 |
| 4               | 127.86 | 101.7994 | 4               | 120.82 | 96.19427 | 4                | 108.75 | 86.58439 |
| 5               | 130.08 | 103.5669 | 5               | 123.28 | 98.15287 | 5                | 109.1  | 86.86306 |
| 6               | 132.39 | 105.4061 | 6               | 128.42 | 102.2452 | 6                | 113.62 | 90.46178 |
| 7               | 132.68 | 105.6369 | 7               | 130.41 | 103.8296 | 7                | 117.26 | 93.35987 |
| 8               | 132.71 | 105.6608 | 8               | 134.03 | 106.7118 | 8                | 119.76 | 95.35032 |
| 9               | 133.4  | 106.2102 | 9               | 134.54 | 107.1178 | 9                | 119.81 | 95.39013 |
| 10              | 136.67 | 108.8137 | 10              | 136.64 | 108.7898 | 10               | 122.91 | 97.85828 |
| 11              | 137.61 | 109.5621 | 11              | 137.88 | 109.7771 | 11               | 125.66 | 100.0478 |
| 12              | 138.13 | 109.9761 | 12              | 139.74 | 111.258  | 12               | 130.03 | 103.5271 |
| 13              | 139.82 | 111.3217 | 13              | 140.05 | 111.5048 | 13               | 130.22 | 103.6783 |
| 14              | 141.26 | 112.4682 | 14              | 141.15 | 112.3806 | 14               | 132.69 | 105.6449 |
| 15              | 141.27 | 112.4761 | 15              | 149.57 | 119.0844 | 15               | 134.21 | 106.8551 |
| 16              | 142.04 | 113.0892 | 16              | 151.57 | 120.6768 | 16               | 137.82 | 109.7293 |
| 17              | 143.04 | 113.8854 | 17              | 153.29 | 122.0462 | 17               | 140.27 | 111.6799 |
| 18              | 151.77 | 120.836  | 18              | 155.17 | 123.543  | 18               | 142.81 | 113.7022 |
| 19              | 159.75 | 127.1895 | 19              | 155.83 | 124.0685 | 19               | 152.68 | 121.5605 |
| 20              | 163.74 | 130.3662 | 20              | 159.03 | 126.6162 | 20               | 160.34 | 127.6592 |
|                 | SUM    | 2195.104 |                 | SUM    | 2183.097 |                  | SUM    | 1998.758 |
|                 | AVG    | 109.7552 |                 | AVG    | 109.1549 |                  | AVG    | 99.9379  |
|                 | STD    | 8.52999  |                 | STD    | 10.77778 |                  | STD    | 12.60263 |

Table A3: Air +149µm Glass Data

| AB +149 1 mm/min |        |          | AB +149 7 mm/min |        |          | AB +149 20 mm/min |        |          |
|------------------|--------|----------|------------------|--------|----------|-------------------|--------|----------|
|                  | P      | MOR      |                  | P      | MOR      |                   | P      | MOR      |
| 1                | 99.88  | 79.52229 | 1                | 106.88 | 85.09554 | 1                 | 112.48 | 89.55414 |
| 2                | 111.82 | 89.02866 | 2                | 113.24 | 90.15924 | 2                 | 121.81 | 96.98248 |
| 3                | 120.21 | 95.7086  | 3                | 117.27 | 93.36783 | 3                 | 127.68 | 101.6561 |
| 4                | 120.42 | 95.8758  | 4                | 121.57 | 96.7914  | 4                 | 137.06 | 109.1242 |
| 5                | 120.93 | 96.28185 | 5                | 130.37 | 103.7978 | 5                 | 139.12 | 110.7643 |
| 6                | 127.79 | 101.7436 | 6                | 134.98 | 107.4682 | 6                 | 145.12 | 115.5414 |
| 7                | 127.98 | 101.8949 | 7                | 137.83 | 109.7373 | 7                 | 145.46 | 115.8121 |
| 8                | 128.6  | 102.3885 | 8                | 138.83 | 110.5334 | 8                 | 147.66 | 117.5637 |
| 9                | 130.15 | 103.6226 | 9                | 141.1  | 112.3408 | 9                 | 150.38 | 119.7293 |
| 10               | 132.98 | 105.8758 | 10               | 141.79 | 112.8901 | 10                | 151.64 | 120.7325 |
| 11               | 133.69 | 106.4411 | 11               | 142.39 | 113.3678 | 11                | 153.52 | 122.2293 |
| 12               | 137.12 | 109.172  | 12               | 144.07 | 114.7054 | 12                | 155.27 | 123.6226 |
| 13               | 139.44 | 111.0191 | 13               | 150.65 | 119.9443 | 13                | 157.14 | 125.1115 |
| 14               | 141.15 | 112.3806 | 14               | 152.28 | 121.242  | 14                | 159.91 | 127.3169 |
| 15               | 141.84 | 112.9299 | 15               | 154.38 | 122.914  | 15                | 160.29 | 127.6194 |
| 16               | 145.35 | 115.7245 | 16               | 158.49 | 126.1863 | 16                | 163.44 | 130.1274 |
| 17               | 146.79 | 116.871  | 17               | 160.53 | 127.8105 | 17                | 168.16 | 133.8854 |
| 18               | 146.9  | 116.9586 | 18               | 161.74 | 128.7739 | 18                | 172.41 | 137.2691 |
| 19               | 148.71 | 118.3997 | 19               | 168.7  | 134.3153 | 19                | 175.05 | 139.371  |
| 20               | 162.14 | 129.0924 | 20               | 174.33 | 138.7978 | 20                | 177.3  | 141.1624 |
|                  | SUM    | 2120.932 |                  | SUM    | 2270.239 |                   | SUM    | 2405.175 |
|                  | AVG    | 106.0466 |                  | AVG    | 113.5119 |                   | AVG    | 120.2588 |
|                  | STD    | 11.15709 |                  | STD    | 14.23923 |                   | STD    | 13.43865 |

Table A4: Air IOX 4hr Glass Data

| IOX 4hr 1 mm/min |        |          | IOX 4hr 7 mm/min |        |          | IOX 4hr 20 mm/min |        |          |
|------------------|--------|----------|------------------|--------|----------|-------------------|--------|----------|
|                  | P      | MOR      |                  | P      | MOR      |                   | P      | MOR      |
| 1                | 438.2  | 348.8854 | 1                | 449.73 | 358.0653 | 1                 | 476.25 | 379.1799 |
| 2                | 465.07 | 370.2787 | 2                | 491.67 | 391.457  | 2                 | 497.52 | 396.1146 |
| 3                | 521.92 | 415.5414 | 3                | 510.92 | 406.7834 | 3                 | 513.71 | 409.0048 |
| 4                | 540.19 | 430.0876 | 4                | 518.89 | 413.129  | 4                 | 532.54 | 423.9968 |
| 5                | 541.66 | 431.258  | 5                | 536.77 | 427.3646 | 5                 | 540.27 | 430.1513 |
| 6                | 558.45 | 444.6258 | 6                | 547.51 | 435.9156 | 6                 | 575.19 | 457.9538 |
| 7                | 558.93 | 445.008  | 7                | 574.37 | 457.301  | 7                 | 584.52 | 465.3822 |
| 8                | 559.86 | 445.7484 | 8                | 586.25 | 466.7596 | 8                 | 584.82 | 465.621  |
| 9                | 560.65 | 446.3774 | 9                | 591    | 470.5414 | 9                 | 590.15 | 469.8646 |
| 10               | 561.11 | 446.7436 | 10               | 604.92 | 481.6242 | 10                | 610.93 | 486.4092 |
| 11               | 562.09 | 447.5239 | 11               | 606.57 | 482.9379 | 11                | 613.23 | 488.2404 |
| 12               | 565.22 | 450.0159 | 12               | 617.07 | 491.2978 | 12                | 625.57 | 498.0653 |
| 13               | 566.26 | 450.8439 | 13               | 618.02 | 492.0541 | 13                | 629.94 | 501.5446 |
| 14               | 567.08 | 451.4968 | 14               | 625.01 | 497.6194 | 14                | 659.84 | 525.3503 |
| 15               | 586.01 | 466.5685 | 15               | 626.42 | 498.742  | 15                | 662.71 | 527.6354 |
| 16               | 587.31 | 467.6035 | 16               | 629.09 | 500.8678 | 16                | 685.02 | 545.3981 |
| 17               | 598.45 | 476.4729 | 17               | 630.16 | 501.7197 | 17                | 693.33 | 552.0143 |
| 18               | 610.7  | 486.2261 | 18               | 649.11 | 516.8073 | 18                | 720.02 | 573.2643 |
| 19               | 619.88 | 493.535  | 19               | 654.68 | 521.242  | 19                | 725.36 | 577.5159 |
| 20               | 624.26 | 497.0223 | 20               | 666.68 | 530.7962 | 20                | 732.88 | 583.5032 |
|                  | SUM    | 8911.863 |                  | SUM    | 9343.025 |                   | SUM    | 9756.21  |
|                  | AVG    | 445.5932 |                  | AVG    | 467.1513 |                   | AVG    | 487.8105 |
|                  | STD    | 35.30938 |                  | STD    | 45.94646 |                   | STD    | 59.69124 |

Table A5: Air IOX 16hr Glass Data

| IOX 16hr 1 mm/min |        |          | IOX 16hr 7 mm/min |        |          | IOX 16hr 20 mm/min |        |          |
|-------------------|--------|----------|-------------------|--------|----------|--------------------|--------|----------|
|                   | P      | MOR      |                   | P      | MOR      |                    | P      | MOR      |
| 1                 | 392.57 | 312.5557 | 1                 | 405.1  | 322.5318 | 1                  | 368.02 | 293.0096 |
| 2                 | 429.49 | 341.9506 | 2                 | 407.37 | 324.3392 | 2                  | 414.73 | 330.199  |
| 3                 | 434.37 | 345.836  | 3                 | 409.51 | 326.043  | 3                  | 415.59 | 330.8838 |
| 4                 | 450.88 | 358.9809 | 4                 | 418.34 | 333.0732 | 4                  | 435.27 | 346.5525 |
| 5                 | 459.85 | 366.1226 | 5                 | 424.27 | 337.7946 | 5                  | 455.1  | 362.3408 |
| 6                 | 464.79 | 370.0557 | 6                 | 427.29 | 340.199  | 6                  | 455.17 | 362.3965 |
| 7                 | 472.41 | 376.1226 | 7                 | 431.46 | 343.5191 | 7                  | 468.03 | 372.6354 |
| 8                 | 485.13 | 386.25   | 8                 | 435.54 | 346.7675 | 8                  | 468.22 | 372.7866 |
| 9                 | 488.59 | 389.0048 | 9                 | 438.02 | 348.742  | 9                  | 470.65 | 374.7213 |
| 10                | 497.53 | 396.1226 | 10                | 438.72 | 349.2994 | 10                 | 474.75 | 377.9857 |
| 11                | 513.01 | 408.4475 | 11                | 443.75 | 353.3041 | 11                 | 482.52 | 384.172  |
| 12                | 514.64 | 409.7452 | 12                | 446.59 | 355.5653 | 12                 | 489.32 | 389.586  |
| 13                | 518.42 | 412.7548 | 13                | 454.4  | 361.7834 | 13                 | 492.06 | 391.7675 |
| 14                | 518.8  | 413.0573 | 14                | 461.7  | 367.5955 | 14                 | 494.08 | 393.3758 |
| 15                | 522.75 | 416.2022 | 15                | 471.07 | 375.0557 | 15                 | 496.54 | 395.3344 |
| 16                | 526.59 | 419.2596 | 16                | 474.77 | 378.0016 | 16                 | 497.31 | 395.9475 |
| 17                | 532.31 | 423.8137 | 17                | 483.39 | 384.8646 | 17                 | 500.45 | 398.4475 |
| 18                | 532.82 | 424.2197 | 18                | 486.22 | 387.1178 | 18                 | 511.47 | 407.2213 |
| 19                | 533.64 | 424.8726 | 19                | 489.23 | 389.5143 | 19                 | 519.35 | 413.4952 |
| 20                | 535.03 | 425.9793 | 20                | 496.06 | 394.9522 | 20                 | 533.61 | 424.8487 |
|                   | SUM    | 7821.354 |                   | SUM    | 7120.064 |                    | SUM    | 7517.707 |
|                   | AVG    | 391.0677 |                   | AVG    | 356.0032 |                    | AVG    | 375.8854 |
|                   | STD    | 32.05969 |                   | STD    | 22.28206 |                    | STD    | 30.92792 |

Table A6: Air IOX 4hr +63µm Glass Data

| IOX 4hr +63 1 mm/min |        |          | IOX 4hr +63 7 mm/min |        |          | IOX 4hr +63 20 mm/min |        |          |
|----------------------|--------|----------|----------------------|--------|----------|-----------------------|--------|----------|
|                      | P      | MOR      |                      | P      | MOR      |                       | P      | MOR      |
| 1                    | 227.54 | 181.1624 | 1                    | 227.33 | 180.9952 | 1                     | 168.66 | 134.2834 |
| 2                    | 253.17 | 201.5685 | 2                    | 257.57 | 205.0717 | 2                     | 249.34 | 198.5191 |
| 3                    | 274.87 | 218.8455 | 3                    | 297.22 | 236.6401 | 3                     | 336.4  | 267.8344 |
| 4                    | 277.99 | 221.3296 | 4                    | 307.22 | 244.6019 | 4                     | 346.62 | 275.9713 |
| 5                    | 396.16 | 315.414  | 5                    | 351.45 | 279.8169 | 5                     | 352.68 | 280.7962 |
| 6                    | 397.83 | 316.7436 | 6                    | 360.58 | 287.086  | 6                     | 363.17 | 289.1481 |
| 7                    | 398.33 | 317.1417 | 7                    | 377.49 | 300.5494 | 7                     | 374.92 | 298.5032 |
| 8                    | 430.46 | 342.7229 | 8                    | 417.82 | 332.6592 | 8                     | 375.32 | 298.8217 |
| 9                    | 431.54 | 343.5828 | 9                    | 425.33 | 338.6385 | 9                     | 396.34 | 315.5573 |
| 10                   | 444    | 353.5032 | 10                   | 427.49 | 340.3583 | 10                    | 422.45 | 336.3455 |
| 11                   | 459.92 | 366.1783 | 11                   | 434.36 | 345.828  | 11                    | 434.63 | 346.043  |
| 12                   | 462.16 | 367.9618 | 12                   | 446.69 | 355.6449 | 12                    | 454.46 | 361.8312 |
| 13                   | 468.79 | 373.2404 | 13                   | 451.54 | 359.5064 | 13                    | 459.75 | 366.043  |
| 14                   | 471.75 | 375.5971 | 14                   | 485.65 | 386.664  | 14                    | 461.79 | 367.6672 |
| 15                   | 476.41 | 379.3073 | 15                   | 492.99 | 392.508  | 15                    | 462.94 | 368.5828 |
| 16                   | 482.54 | 384.1879 | 16                   | 498.04 | 396.5287 | 16                    | 500.42 | 398.4236 |
| 17                   | 486.96 | 387.707  | 17                   | 525.51 | 418.3997 | 17                    | 503.16 | 400.6051 |
| 18                   | 494.47 | 393.6863 | 18                   | 526.45 | 419.1481 | 18                    | 534.89 | 425.8678 |
| 19                   | 502.03 | 399.7054 | 19                   | 545.88 | 434.6178 | 19                    | 538.57 | 428.7978 |
| 20                   | 536.86 | 427.4363 | 20                   | 547.59 | 435.9793 | 20                    |        | 0        |
|                      | SUM    | 6667.022 |                      | SUM    | 6691.242 |                       | SUM    | 6159.642 |
|                      | AVG    | 333.3511 |                      | AVG    | 334.5621 |                       | AVG    | 324.1917 |
|                      | STD    | 69.94458 |                      | STD    | 74.18887 |                       | STD    | 100.4934 |

Table A7: Air IOX 4hr +149µm Glass Data

| IOX 4hr +149 1 mm/min |        |          | IOX 4hr +149 7 mm/min |        |          | IOX 4hr +149 20 mm/min |        |          |
|-----------------------|--------|----------|-----------------------|--------|----------|------------------------|--------|----------|
|                       | P      | MOR      |                       | P      | MOR      |                        | P      | MOR      |
| 1                     | 119.37 | 95.03981 | 1                     | 109.91 | 87.50796 | 1                      | 183.84 | 146.3694 |
| 2                     | 177.5  | 141.3217 | 2                     | 133.09 | 105.9634 | 2                      | 216.18 | 172.1178 |
| 3                     | 188.26 | 149.8885 | 3                     | 191.48 | 152.4522 | 3                      | 239.37 | 190.5812 |
| 4                     | 193.62 | 154.1561 | 4                     | 219.67 | 174.8965 | 4                      | 263.46 | 209.7611 |
| 5                     | 203.92 | 162.3567 | 5                     | 257.5  | 205.0159 | 5                      | 279.63 | 222.6354 |
| 6                     | 239.65 | 190.8041 | 6                     | 267.37 | 212.8742 | 6                      | 326.82 | 260.207  |
| 7                     | 276.42 | 220.0796 | 7                     | 303.36 | 241.5287 | 7                      | 368.64 | 293.5032 |
| 8                     | 287.69 | 229.0525 | 8                     | 307.9  | 245.1433 | 8                      | 401.23 | 319.4506 |
| 9                     | 292.96 | 233.2484 | 9                     | 320.78 | 255.3981 | 9                      | 410.41 | 326.7596 |
| 10                    | 298.27 | 237.4761 | 10                    | 328.28 | 261.3694 | 10                     | 427.13 | 340.0717 |
| 11                    | 336.07 | 267.5717 | 11                    | 335.32 | 266.9745 | 11                     | 449.36 | 357.7707 |
| 12                    | 343.19 | 273.2404 | 12                    | 384.92 | 306.465  | 12                     | 452.02 | 359.8885 |
| 13                    | 387.19 | 308.2723 | 13                    | 385.22 | 306.7038 | 13                     | 454.33 | 361.7277 |
| 14                    | 401.12 | 319.3631 | 14                    | 414.49 | 330.008  | 14                     | 465.1  | 370.3025 |
| 15                    | 401.72 | 319.8408 | 15                    | 432.67 | 344.4825 | 15                     | 473.43 | 376.9347 |
| 16                    | 421.95 | 335.9475 | 16                    | 450.13 | 358.3838 | 16                     | 475.76 | 378.7898 |
| 17                    | 460    | 366.242  | 17                    | 457.26 | 364.0605 | 17                     | 487.78 | 388.3599 |
| 18                    | 464.34 | 369.6975 | 18                    | 471.61 | 375.4857 | 18                     | 506.03 | 402.8901 |
| 19                    | 464.9  | 370.1433 | 19                    | 494.13 | 393.4156 | 19                     | 581.63 | 463.0812 |
| 20                    |        | 0        | 20                    | 512.72 | 408.2166 | 20                     | 584.87 | 465.6608 |
|                       | SUM    | 4743.742 |                       | SUM    | 5396.346 |                        | SUM    | 6406.863 |
|                       | AVG    | 249.6706 |                       | AVG    | 269.8173 |                        | AVG    | 320.3432 |
|                       | STD    | 97.67297 |                       | STD    | 91.16782 |                        | STD    | 90.09507 |

Table A8: Air IOX 16hr +63µm Glass Data

| IOX 16hr +63 1 mm/min |        |          | IOX 16hr +63 7mm/min |        |          | IOX 16hr +63 20 mm/min |        |          |
|-----------------------|--------|----------|----------------------|--------|----------|------------------------|--------|----------|
|                       | P      | MOR      |                      | P      | MOR      |                        | P      | MOR      |
| 1                     | 406.5  | 323.6465 | 1                    | 248.73 | 198.0334 | 1                      | 325.17 | 258.8933 |
| 2                     | 453.91 | 361.3933 | 2                    | 299.72 | 238.6306 | 2                      | 346.02 | 275.4936 |
| 3                     | 455.82 | 362.914  | 3                    | 359.68 | 286.3694 | 3                      | 348.88 | 277.7707 |
| 4                     | 479.49 | 381.7596 | 4                    | 463.62 | 369.1242 | 4                      | 355.51 | 283.0494 |
| 5                     | 488.33 | 388.7978 | 5                    | 468.42 | 372.9459 | 5                      | 372.12 | 296.2739 |
| 6                     | 491.46 | 391.2898 | 6                    | 498.04 | 396.5287 | 6                      | 392.93 | 312.8424 |
| 7                     | 495.83 | 394.7691 | 7                    | 500.1  | 398.1688 | 7                      | 407.62 | 324.5382 |
| 8                     | 520.44 | 414.3631 | 8                    | 510.27 | 406.2659 | 8                      | 407.8  | 324.6815 |
| 9                     | 520.9  | 414.7293 | 9                    | 522.42 | 415.9395 | 9                      | 408.52 | 325.2548 |
| 10                    | 527.64 | 420.0955 | 10                   | 529.43 | 421.5207 | 10                     | 412.88 | 328.7261 |
| 11                    | 529.73 | 421.7596 | 11                   | 530.93 | 422.715  | 11                     | 418.66 | 333.328  |
| 12                    | 542.84 | 432.1975 | 12                   | 532.1  | 423.6465 | 12                     | 432.39 | 344.2596 |
| 13                    | 554.03 | 441.1067 | 13                   | 540.72 | 430.5096 | 13                     | 434.18 | 345.6847 |
| 14                    | 555.33 | 442.1417 | 14                   | 546.25 | 434.9124 | 14                     | 438.36 | 349.0127 |
| 15                    | 559.79 | 445.6927 | 15                   | 546.37 | 435.008  | 15                     | 440.52 | 350.7325 |
| 16                    | 568.03 | 452.2532 | 16                   | 563.91 | 448.9729 | 16                     | 443.84 | 353.3758 |
| 17                    | 569.53 | 453.4475 | 17                   | 566.19 | 450.7882 | 17                     | 447.31 | 356.1385 |
| 18                    | 581.53 | 463.0016 | 18                   | 567.36 | 451.7197 | 18                     | 465.72 | 370.7962 |
| 19                    | 583.76 | 464.7771 | 19                   | 578.52 | 460.6051 | 19                     | 470.76 | 374.8089 |
| 20                    | 600.88 | 478.4076 | 20                   | 582.37 | 463.6704 | 20                     | 471.46 | 375.3662 |
|                       | SUM    | 8348.543 |                      | SUM    | 7926.075 |                        | SUM    | 6561.027 |
|                       | AVG    | 417.4271 |                      | AVG    | 396.3037 |                        | AVG    | 328.0514 |
|                       | STD    | 39.35341 |                      | STD    | 71.32895 |                        | STD    | 33.62229 |

Table A9: Air IOX 16hr +149µm Glass Data

| IOX 16hr +149 1 mm/min |        |          | IOX 16hr +149 7 mm/min |        |          | IOX 16hr +149 20 mm/min |        |          |
|------------------------|--------|----------|------------------------|--------|----------|-------------------------|--------|----------|
|                        | P      | MOR      |                        | P      | MOR      |                         | P      | MOR      |
| 1                      | 207.92 | 165.5414 | 1                      | 287.94 | 229.2516 | 1                       | 153.21 | 121.9825 |
| 2                      | 291    | 231.6879 | 2                      | 348.19 | 277.2213 | 2                       | 252.48 | 201.0191 |
| 3                      | 317.78 | 253.0096 | 3                      | 399.86 | 318.3599 | 3                       | 337.32 | 268.5669 |
| 4                      | 325.75 | 259.3551 | 4                      | 435.93 | 347.078  | 4                       | 374.9  | 298.4873 |
| 5                      | 329.26 | 262.1497 | 5                      | 463.63 | 369.1322 | 5                       | 404.88 | 322.3567 |
| 6                      | 359.52 | 286.242  | 6                      | 469.26 | 373.6146 | 6                       | 407.12 | 324.1401 |
| 7                      | 438.3  | 348.965  | 7                      | 509.21 | 405.422  | 7                       | 412.11 | 328.1131 |
| 8                      | 441.37 | 351.4092 | 8                      | 514.05 | 409.2755 | 8                       | 418.87 | 333.4952 |
| 9                      | 449.6  | 357.9618 | 9                      | 515.25 | 410.2309 | 9                       | 420.32 | 334.6497 |
| 10                     | 453.52 | 361.0828 | 10                     | 515.35 | 410.3105 | 10                      | 421.82 | 335.8439 |
| 11                     | 471.31 | 375.2468 | 11                     | 525.76 | 418.5987 | 11                      | 423.18 | 336.9268 |
| 12                     | 471.85 | 375.6768 | 12                     | 525.9  | 418.7102 | 12                      | 423.62 | 337.2771 |
| 13                     | 475.48 | 378.5669 | 13                     | 530.67 | 422.508  | 13                      | 428.03 | 340.7882 |
| 14                     | 479.75 | 381.9666 | 14                     | 540.07 | 429.992  | 14                      | 429.46 | 341.9268 |
| 15                     | 490.23 | 390.3105 | 15                     | 541.18 | 430.8758 | 15                      | 433.41 | 345.0717 |
| 16                     | 491.94 | 391.672  | 16                     | 547.78 | 436.1306 | 16                      | 441.63 | 351.6162 |
| 17                     | 510.17 | 406.1863 | 17                     | 555.1  | 441.9586 | 17                      | 442.98 | 352.6911 |
| 18                     | 533.88 | 425.0637 | 18                     | 578.21 | 460.3583 | 18                      | 455.06 | 362.3089 |
| 19                     | 551.95 | 439.4506 | 19                     | 578.97 | 460.9634 | 19                      | 458.42 | 364.9841 |
| 20                     | 555.92 | 442.6115 | 20                     | 592.7  | 471.8949 | 20                      | 472.64 | 376.3057 |
|                        | SUM    | 6884.156 |                        | SUM    | 7941.887 |                         | SUM    | 6378.551 |
|                        | AVG    | 344.2078 |                        | AVG    | 397.0943 |                         | AVG    | 318.9275 |
|                        | STD    | 73.76086 |                        | STD    | 60.89004 |                         | STD    | 58.46692 |

Table A10: Water As Received Glass Data

| Nothing | 0.2 mm/min |         | Nothing | 2 mm/min |         | Nothing | 20 mm/min |         |
|---------|------------|---------|---------|----------|---------|---------|-----------|---------|
|         | P          | MOR     |         | P        | MOR     |         | P         | MOR     |
| 1       | 104.80     | 83.44   | 1.00    | 90.67    | 72.19   | 1.00    | 105.01    | 83.61   |
| 2       | 108.92     | 86.72   | 2.00    | 95.20    | 75.80   | 2.00    | 105.84    | 84.27   |
| 3       | 115.01     | 91.57   | 3.00    | 105.00   | 83.60   | 3.00    | 107.72    | 85.76   |
| 4       | 118.84     | 94.62   | 4.00    | 108.34   | 86.26   | 4.00    | 108.73    | 86.57   |
| 5       | 119.26     | 94.95   | 5.00    | 109.79   | 87.41   | 5.00    | 111.28    | 88.60   |
| 6       | 122.61     | 97.62   | 6.00    | 112.43   | 89.51   | 6.00    | 112.78    | 89.79   |
| 7       | 123.33     | 98.19   | 7.00    | 115.45   | 91.92   | 7.00    | 115.77    | 92.17   |
| 8       | 128.71     | 102.48  | 8.00    | 119.28   | 94.97   | 8.00    | 127.97    | 101.89  |
| 9       | 129.78     | 103.33  | 9.00    | 121.84   | 97.01   | 9.00    | 130.25    | 103.70  |
| 10      | 130.51     | 103.91  | 10.00   | 126.96   | 101.08  | 10.00   | 132.73    | 105.68  |
| 11      | 134.70     | 107.25  | 11.00   | 129.37   | 103.00  | 11.00   | 132.99    | 105.88  |
| 12      | 135.05     | 107.52  | 12.00   | 131.78   | 104.92  | 12.00   | 135.29    | 107.71  |
| 13      | 135.09     | 107.56  | 13.00   | 134.60   | 107.17  | 13.00   | 143.31    | 114.10  |
| 14      | 135.30     | 107.72  | 14.00   | 136.33   | 108.54  | 14.00   | 144.91    | 115.37  |
| 15      | 135.52     | 107.90  | 15.00   | 136.87   | 108.97  | 15.00   | 145.33    | 115.71  |
| 16      | 136.52     | 108.69  | 16.00   | 137.94   | 109.82  | 16.00   | 153.26    | 122.02  |
| 17      | 137.90     | 109.79  | 17.00   | 141.70   | 112.82  | 17.00   | 156.79    | 124.83  |
| 18      | 143.41     | 114.18  | 18.00   | 155.86   | 124.09  | 18.00   | 159.41    | 126.92  |
| 19      | 144.09     | 114.72  | 19.00   | 157.02   | 125.02  | 19.00   | 167.02    | 132.98  |
| 20      | 162.31     | 129.23  | 20.00   | 158.70   | 126.35  | 20.00   | 167.80    | 133.60  |
|         | SUM        | 2071.39 |         | SUM      | 2010.45 |         | SUM       | 2121.17 |
|         | AVG        | 103.57  |         | AVG      | 100.52  |         | AVG       | 106.06  |
|         | STD        | 10.23   |         | STD      | 15.13   |         | STD       | 16.32   |

Table A11: Water +149µm Glass Data

| 149+ | 0.2 mm/min |          | 149+ | 2 mm/min |          | 149+ | 20 mm/min |          |
|------|------------|----------|------|----------|----------|------|-----------|----------|
|      | P          | MOR      |      | P        | MOR      |      | P         | MOR      |
| 1    | 80.65      | 64.21178 | 1    | 86.26    | 68.67834 | 1    | 86.67     | 69.00478 |
| 2    | 85.08      | 67.73885 | 2    | 94.68    | 75.38217 | 2    | 94.75     | 75.4379  |
| 3    | 91.89      | 73.16083 | 3    | 99.98    | 79.60191 | 3    | 96.94     | 77.18153 |
| 4    | 92.25      | 73.44745 | 4    | 100.82   | 80.2707  | 4    | 99.19     | 78.97293 |
| 5    | 95.67      | 76.17038 | 5    | 102.17   | 81.34554 | 5    | 102.2     | 81.36943 |
| 6    | 96.41      | 76.75955 | 6    | 102.33   | 81.47293 | 6    | 107.94    | 85.93949 |
| 7    | 98.1       | 78.1051  | 7    | 108.43   | 86.32962 | 7    | 108.07    | 86.04299 |
| 8    | 98.43      | 78.36783 | 8    | 110.53   | 88.00159 | 8    | 110.74    | 88.16879 |
| 9    | 98.77      | 78.63854 | 9    | 111.36   | 88.66242 | 9    | 111.76    | 88.98089 |
| 10   | 103.01     | 82.01433 | 10   | 111.71   | 88.94108 | 10   | 112.02    | 89.1879  |
| 11   | 103.04     | 82.03822 | 11   | 112.87   | 89.86465 | 11   | 112.47    | 89.54618 |
| 12   | 103.09     | 82.07803 | 12   | 113.49   | 90.35828 | 12   | 113.4     | 90.28662 |
| 13   | 105.99     | 84.38694 | 13   | 114.15   | 90.88376 | 13   | 114.35    | 91.04299 |
| 14   | 106.29     | 84.6258  | 14   | 114.57   | 91.21815 | 14   | 118.14    | 94.06051 |
| 15   | 110.42     | 87.91401 | 15   | 114.86   | 91.44904 | 15   | 119.38    | 95.04777 |
| 16   | 111.22     | 88.55096 | 16   | 115.32   | 91.81529 | 16   | 119.43    | 95.08758 |
| 17   | 113.73     | 90.54936 | 17   | 116.79   | 92.98567 | 17   | 122.48    | 97.51592 |
| 18   | 113.87     | 90.66083 | 18   | 116.93   | 93.09713 | 18   | 124.45    | 99.08439 |
| 19   | 116.78     | 92.97771 | 19   | 119.98   | 95.52548 | 19   | 126.59    | 100.7882 |
| 20   | 120.69     | 96.09076 | 20   | 120.12   | 95.63694 | 20   | 127.83    | 101.7755 |
|      | SUM        | 1628.487 |      | SUM      | 1741.521 |      | SUM       | 1774.522 |
|      | AVG        | 81.42436 |      | AVG      | 87.07604 |      | AVG       | 88.72611 |
|      | STD        | 8.133916 |      | STD      | 6.91624  |      | STD       | 8.60605  |

Table A12: Water IOX 16hr Glass Data

| IOX 16hr | 0.2 mm/min |          | IOX 16hr | 2 mm/min |          | IOX 16hr | 20 mm/min |          |
|----------|------------|----------|----------|----------|----------|----------|-----------|----------|
|          | P          | MOR      |          | P        | MOR      |          | P         | MOR      |
| 1        | 370.7      | 295.1433 | 1        | 434.07   | 345.5971 | 1        | 407.51    | 324.4506 |
| 2        | 381.07     | 303.3997 | 2        | 440.1    | 350.3981 | 2        | 418.4     | 333.121  |
| 3        | 400.68     | 319.0127 | 3        | 442.46   | 352.2771 | 3        | 422.45    | 336.3455 |
| 4        | 415.45     | 330.7723 | 4        | 444.68   | 354.0446 | 4        | 429.61    | 342.0462 |
| 5        | 421.98     | 335.9713 | 5        | 448.67   | 357.2213 | 5        | 433.32    | 345      |
| 6        | 426.2      | 339.3312 | 6        | 451.15   | 359.1959 | 6        | 440.27    | 350.5334 |
| 7        | 443.2      | 352.8662 | 7        | 457.82   | 364.5064 | 7        | 450.98    | 359.0605 |
| 8        | 453.1      | 360.7484 | 8        | 463.67   | 369.164  | 8        | 458.24    | 364.8408 |
| 9        | 462.48     | 368.2166 | 9        | 475.88   | 378.8854 | 9        | 459.25    | 365.6449 |
| 10       | 466.08     | 371.0828 | 10       | 477.73   | 380.3583 | 10       | 459.42    | 365.7803 |
| 11       | 467.01     | 371.8232 | 11       | 485.9    | 386.8631 | 11       | 465.18    | 370.3662 |
| 12       | 468.1      | 372.6911 | 12       | 486.22   | 387.1178 | 12       | 469.98    | 374.1879 |
| 13       | 478.08     | 380.6369 | 13       | 498.84   | 397.1656 | 13       | 490.87    | 390.8201 |
| 14       | 488.61     | 389.0207 | 14       | 502.78   | 400.3025 | 14       | 492.48    | 392.1019 |
| 15       | 490.13     | 390.2309 | 15       | 510.07   | 406.1067 | 15       | 494.38    | 393.6146 |
| 16       | 491.24     | 391.1146 | 16       | 515.86   | 410.7166 | 16       | 503.24    | 400.6688 |
| 17       | 506.5      | 403.2643 | 17       | 524.08   | 417.2611 | 17       | 504.7     | 401.8312 |
| 18       | 509.28     | 405.4777 | 18       | 529.27   | 421.3933 | 18       | 505.03    | 402.0939 |
| 19       | 513.01     | 408.4475 | 19       | 538.55   | 428.7818 | 19       | 535.31    | 426.2022 |
| 20       | 527.24     | 419.7771 | 20       | 543.31   | 432.5717 | 20       | 539.97    | 429.9124 |
|          | SUM        | 7309.029 |          | SUM      | 7699.928 |          | SUM       | 7468.623 |
|          | AVG        | 365.4514 |          | AVG      | 384.9964 |          | AVG       | 373.4311 |
|          | STD        | 34.5743  |          | STD      | 27.37539 |          | STD       | 29.60549 |



Table A13: Water IOX 16hr +149µm Glass Data

| IOX 16hr +149 | 0.2 mm/min |          | IOX 16hr +149 | 2 mm/min |          | IOX 16hr +149 | 20 mm/min |          |
|---------------|------------|----------|---------------|----------|----------|---------------|-----------|----------|
|               | P          | MOR      |               | P        | MOR      |               | P         | MOR      |
| 1             | 218.21     | 173.7341 | 1             | 116.11   | 92.44427 | 1             | 122.39    | 97.44427 |
| 2             | 239.84     | 190.9554 | 2             | 238.36   | 189.7771 | 2             | 145.02    | 115.4618 |
| 3             | 272.11     | 216.6481 | 3             | 287.09   | 228.5748 | 3             | 163.77    | 130.3901 |
| 4             | 317.97     | 253.1608 | 4             | 289.84   | 230.7643 | 4             | 264.85    | 210.8678 |
| 5             | 329.18     | 262.086  | 5             | 312.06   | 248.4554 | 5             | 278.62    | 221.8312 |
| 6             | 333.13     | 265.2309 | 6             | 344.05   | 273.9252 | 6             | 298.32    | 237.5159 |
| 7             | 340.9      | 271.4172 | 7             | 354.64   | 282.3567 | 7             | 342.44    | 272.6433 |
| 8             | 352.54     | 280.6847 | 8             | 364.2    | 289.9682 | 8             | 349.82    | 278.5191 |
| 9             | 358.69     | 285.5812 | 9             | 373.75   | 297.5717 | 9             | 361.65    | 287.9379 |
| 10            | 361.5      | 287.8185 | 10            | 380.05   | 302.5876 | 10            | 363.71    | 289.578  |
| 11            | 366.88     | 292.1019 | 11            | 382.44   | 304.4904 | 11            | 365.55    | 291.043  |
| 12            | 371.19     | 295.5334 | 12            | 384.81   | 306.3774 | 12            | 372.37    | 296.4729 |
| 13            | 371.76     | 295.9873 | 13            | 394.69   | 314.2436 | 13            | 377.68    | 300.7006 |
| 14            | 372.6      | 296.6561 | 14            | 398.28   | 317.1019 | 14            | 377.76    | 300.7643 |
| 15            | 373.49     | 297.3646 | 15            | 403.24   | 321.051  | 15            | 379.96    | 302.5159 |
| 16            | 379.08     | 301.8153 | 16            | 403.93   | 321.6003 | 16            | 384.24    | 305.9236 |
| 17            | 402.22     | 320.2389 | 17            | 404.02   | 321.672  | 17            | 384.33    | 305.9952 |
| 18            | 409.73     | 326.2182 | 18            | 404.13   | 321.7596 | 18            | 385.13    | 306.6322 |
| 19            | 420.61     | 334.8806 | 19            | 404.19   | 321.8073 | 19            | 387.12    | 308.2166 |
| 20            | 429.18     | 341.7038 | 20            | 413.63   | 329.3232 | 20            | 412.3     | 328.2643 |
|               | SUM        | 5589.817 |               | SUM      | 5615.852 |               | SUM       | 5188.718 |
|               | AVG        | 279.4908 |               | AVG      | 280.7926 |               | AVG       | 259.4359 |
|               | STD        | 42.96986 |               | STD      | 57.11867 |               | STD       | 67.61891 |